

1. Increasing / decreasing a quantity by a given percentage.
2. Reverse percentage problems.

1. Increasing / decreasing a quantity by a given percentage.

a. Increase £65 by 14%

First find 14% of £65

$$\text{£}65 \times 0.14 = \text{£}9.10$$

Add this to original

$$\text{£}65 + \text{£}9.10 = \text{£}74.10$$

Alternative method

$$100\% + 14\% = 114\%$$

Find 114% of £65

$$\text{£}65 \times 1.14 = \text{£}74.10$$

b. Increase 125 kg by 32%

Find 132% of 125 kg

$$125 \text{ kg} \times 1.32 = 165 \text{ kg}$$

c. Increase 43 m by 8%

Find 108% of 43 m

$$43 \text{ m} \times 1.08 = 46.44 \text{ m}$$

d. Decrease £84 by 17%

Find 17% of £84

$$\text{£}84 \times 0.17 = \text{£}14.28$$

Subtract this from original

$$\text{£}84 - \text{£}14.28 = \text{£}69.72$$

Alternative method

$$100\% - 17\% = 83\%$$

Find 83% of £84

$$\text{£}84 \times 0.83 = \text{£}69.72$$

e. Decrease 120 kg by 8%

$$100\% - 8\% = 92\%$$

Find 92% of 120 kg

$$120 \text{ kg} \times 0.92 = 110.4 \text{ kg}$$

f. Decrease 400m by 35%

$$100\% - 35\% = 65\%$$

Find 65% of 400m

$$400 \text{ m} \times 0.65 = 260 \text{ m}$$

## 2. Reverse Percentage Problems

If your boss gave you a 10% pay rise and then a 10% pay cut, would your pay then be:

- a. More than before the two changes occurred
- b. Less than before the two changes occurred
- c. The same as before the two changes occurred

Suppose original pay was £100

After 10% pay rise it would be £110

After 10% pay cut it would be £99

So pay would be less than original !!

- a. In a sale with 25% off a coat is priced at £48.

What was the original price before the sale?

$$\text{Original Price} \times 0.75 = £48$$

$$\text{so } £48 \div 0.75 = \text{Original Price}$$

$$\text{£48} \div 0.75 = \text{£64}$$

We can check this is correct by taking 25% off £64  
 25% is £16 and £64 - £16 does give £48.

Notice that adding on 25% of £48 does not give the correct answer 25% of £48 is £12 and £48 + £12 = £60  
 However, if you take off 25% then £60 - £15 = £45 not £48 as required.

- b. After losing 15% of his weight on a diet, a man weighed 68 kg. What was his original weight?

$$\text{Original weight} \times 0.85 = 68 \text{ kg}$$

$$\text{so } 68 \text{ kg} \div 0.85 = \text{original weight}$$

$$68 \text{ kg} \div 0.85 = 80 \text{ kg}$$

- c. A television is priced at £288 inclusive of 20% VAT  
 What is the price exclusive of VAT?

$$\text{Ex VAT price} \times 1.20 = \text{£288}$$

$$\text{so } \text{£288} \div 1.20 = \text{Ex VAT price}$$

$$\text{£288} \div 1.20 = \text{£240}$$

d. After a 5% pay rise John had an hourly rate of pay of £6.72. What was his previous hourly rate of pay?

$$\text{Previous rate} \times 1.05 = £6.72$$

$$\text{so } £6.72 \div 1.05 = \text{Previous rate}$$

$$£6.72 \div 1.05 = £6.40$$

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