

Algebra - Non-Linear Simultaneous Equations

Solve algebraically these simultaneous equations.

$$3x + 2y = 7$$

$$y = x^2 - 2x + 3$$

[7]

Algebra - Non-Linear Simultaneous Equations

Solve algebraically these simultaneous equations.

$$3x + 2y = 7$$

$$y = x^2 - 2x + 3$$

[7]

Substitute for y

$$3x + 2(x^2 - 2x + 3) = 7$$

$$3x + 2x^2 - 4x + 6 - 7 = 0$$

$$2x^2 - x - 1 = 0$$

$$\begin{array}{r} 2x-1 \\ =-2 \end{array} \quad 2x^2 + x - 2x - 1 = 0$$

$$\begin{array}{r} +1-2x \\ -1+2 \end{array} \quad x(2x+1) - 1(2x+1) = 0$$

$$(x-1)(2x+1) = 0$$

Either $x - 1 = 0$
 $x = 1$

or $2x + 1 = 0$
 $2x = -1$
 $x = -\frac{1}{2}$

Substitute for x
when $x = 1$

$$3 + 2y = 7$$

$$2y = 7 - 3$$

$$2y = 4$$

$$y = \frac{4}{2}$$

$$y = 2$$

when $x = -\frac{1}{2}$

$$-\frac{3}{2} + 2y = 7$$

$$2y = 7 + \frac{3}{2}$$

$$2y = \frac{17}{2}$$

$$y = \frac{17}{4}$$

$$\begin{cases} x = 1 \\ y = 2 \end{cases}$$

$$\begin{cases} x = -\frac{1}{2} \\ y = \frac{17}{4} \end{cases} \text{ or } 4\frac{1}{4}$$